

**MATH 113: DISCRETE STRUCTURES  
HOMEWORK 31**

*Problem 1.* What is the remainder of  $10^{100}$  upon division by 13?

*Problem 2.* Consider a regular  $p$ -gon, and for fixed  $k$  (with  $1 \leq k \leq p - 1$ ), consider all  $k$ -subsets (subsets with  $k$  elements) of all of its vertices. Define an equivalence relation on the set of  $k$ -subsets: two  $k$ -subsets are equivalent if one can be rotated into the other one.

- (a) Prove that if  $p$  is prime, then each equivalence class has exactly  $p$  elements.
- (b) Show by an example that (a) is not true if  $p$  is not prime.
- (c) Use (a) to prove that  $p$  divides  $\binom{p}{k}$ .